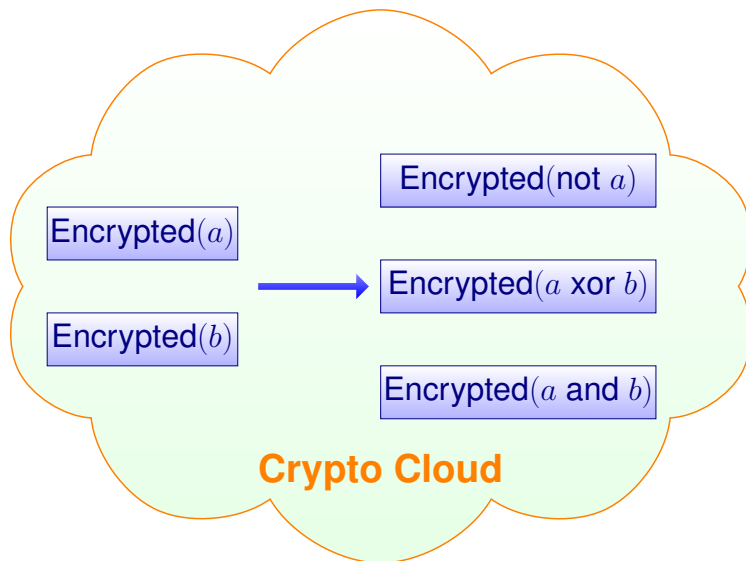
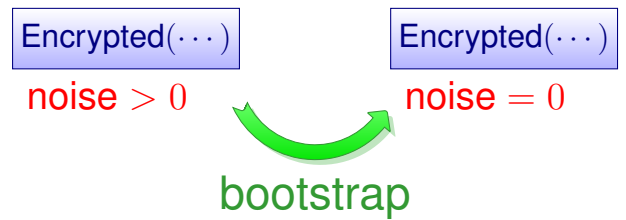


# Optimization of Bootstrapping in Circuits

Hang Zhou



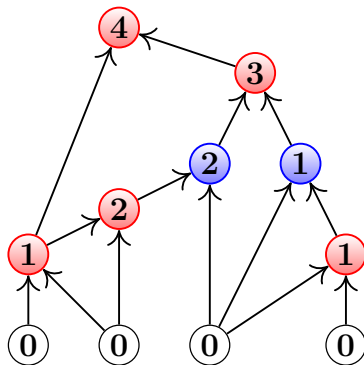
In *fully homomorphic encryption*, the **noise** grows during the computation. To reduce the noise, we use **bootstrap** operations.



## Problem

Minimize the number of bootstrap operations so that the noise is at most  $L \in \mathbb{N}$  at every gate.

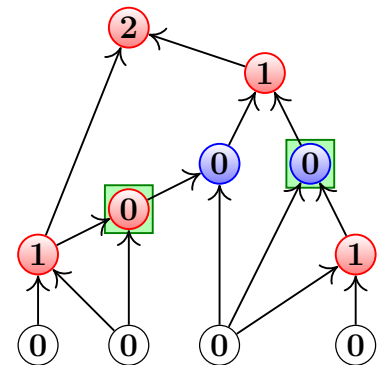
Input (with  $L = 2$ ):



noise calculation:

- $\max(\cdot, \cdot)$
- $1 + \max(\cdot, \cdot)$
- 0

Output:



## Our Results (Benhamouda, Lepoint, Mathieu, Zhou, SODA'17)

- Polynomial-time  $L$ -approximation algorithm
- NP-hard for  $(L - \epsilon)$ -approximation under the Unique Games Conjecture

**Technical novelty:** new rounding scheme for the standard linear program

